

ADAPTIVE SEQUENTIAL MONTE CARLO APPROACH FOR REAL-TIME APPLICATIONS



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Introduction

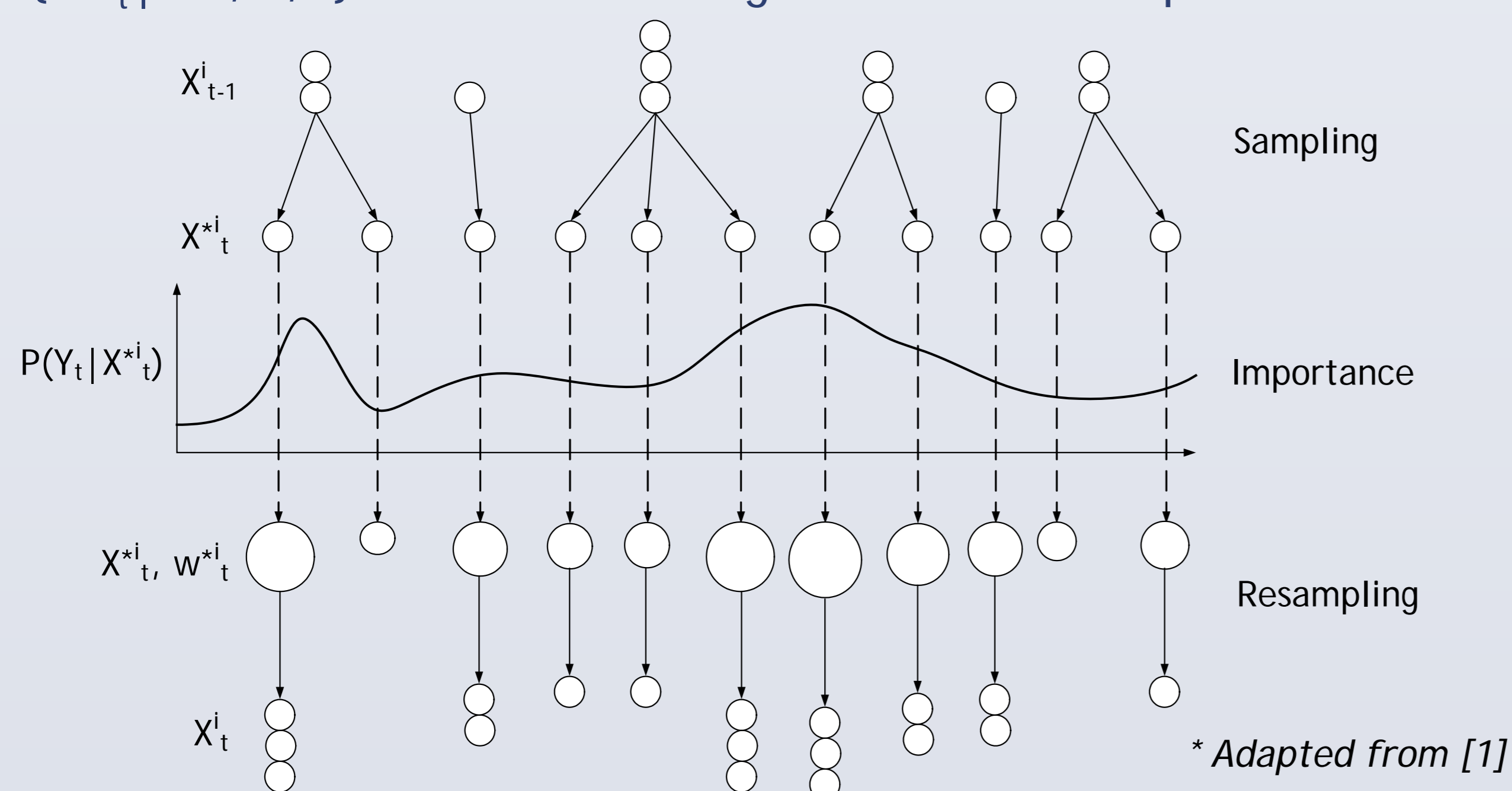
- Sequential Monte Carlo (SMC) methods: estimate states of dynamic systems using weighted particles.
- Adaptive real-time approach: analyse run-time workload for dynamic task allocation to processors on FPGA to improve energy efficiency.
- Example: dynamic energy consumption of robot localisation is reduced by up to 70% without affecting solution quality.

Motivation and Objective

- Real-time systems are often energy constrained.
- Events often occur at regular intervals for real-time applications.
- Objective: reduce energy by exploiting slack time when system is idle.

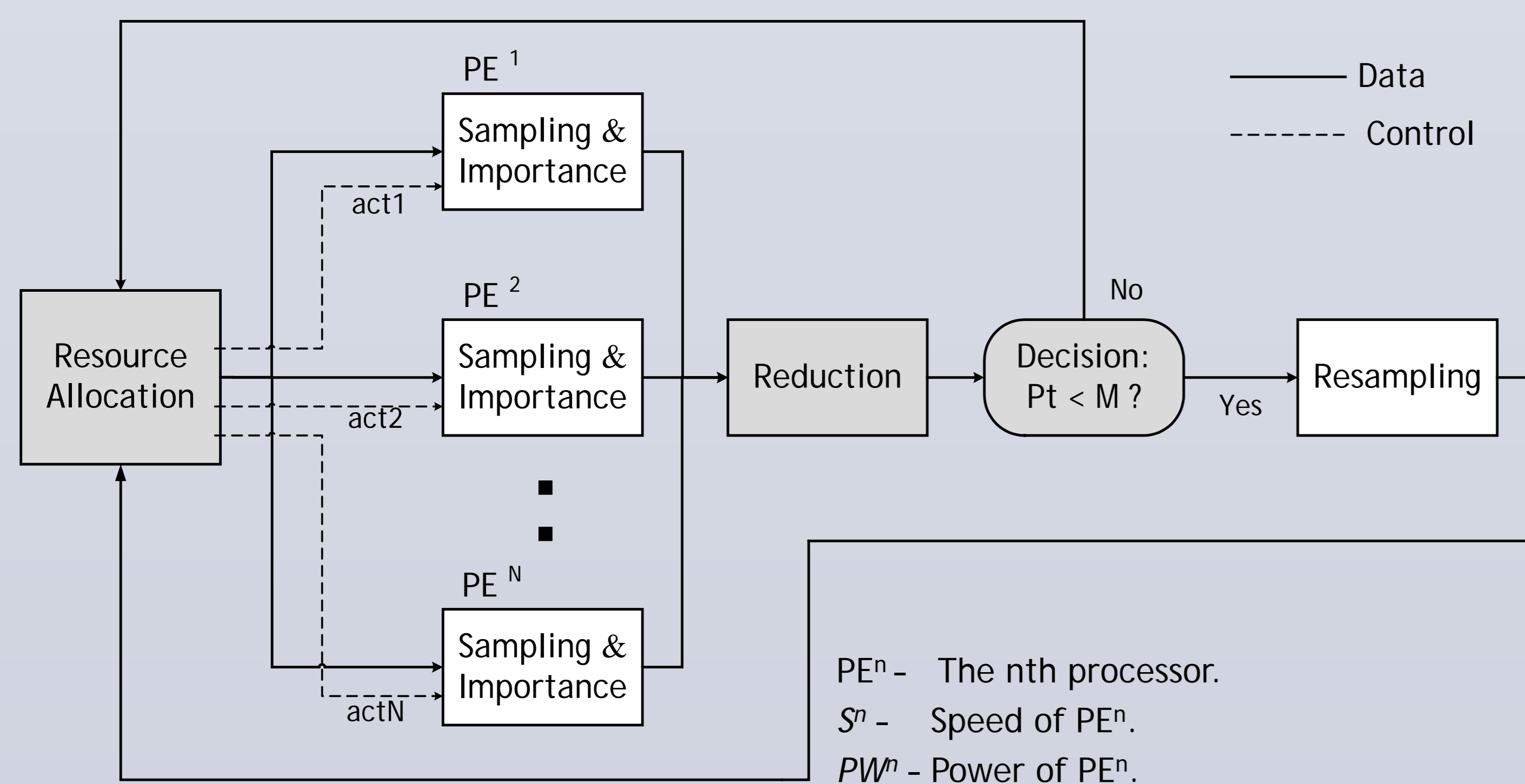
Sequential Monte Carlo Methods

- X_t - State of the system at time t .
- Y_t - Observation of the system at time t .
- $\{x_t^i | i=1, \dots, P\}$ - A set of P particles representing X_t .
- $\{w_t^i | i=1, \dots, P\}$ - Associated weights of the set of particles.



Adaptive SMC Approach

- Sampling and Importance: particles are distributed to N processors for parallel processing.
- Reduction: particles with low weight are eliminated, i.e. workload is reduced.
- Resampling: the set of particles are restored if the particle count (P_t) drops below a threshold (M).
- Resource allocation: particles are distributed to processors which are deactivated after computation finishes.



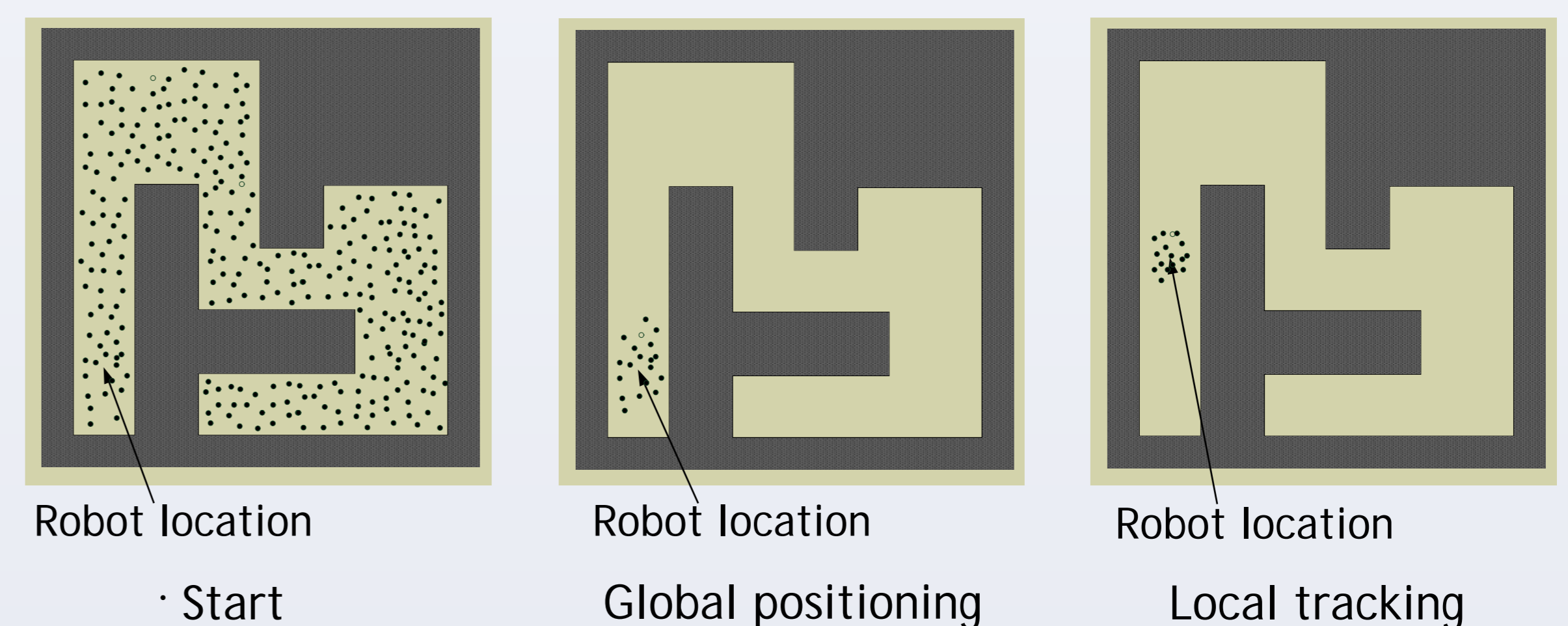
$$\text{Determine } \{\rho^n | n = 1, \dots, N\} = P \cdot \frac{S^n}{\sum_{k=1}^N \frac{S^k}{PW^k}}$$

$$\text{subject to } \sum_{n=1}^N \rho^n = P \text{ and } T(P) \leq T_{RT}$$

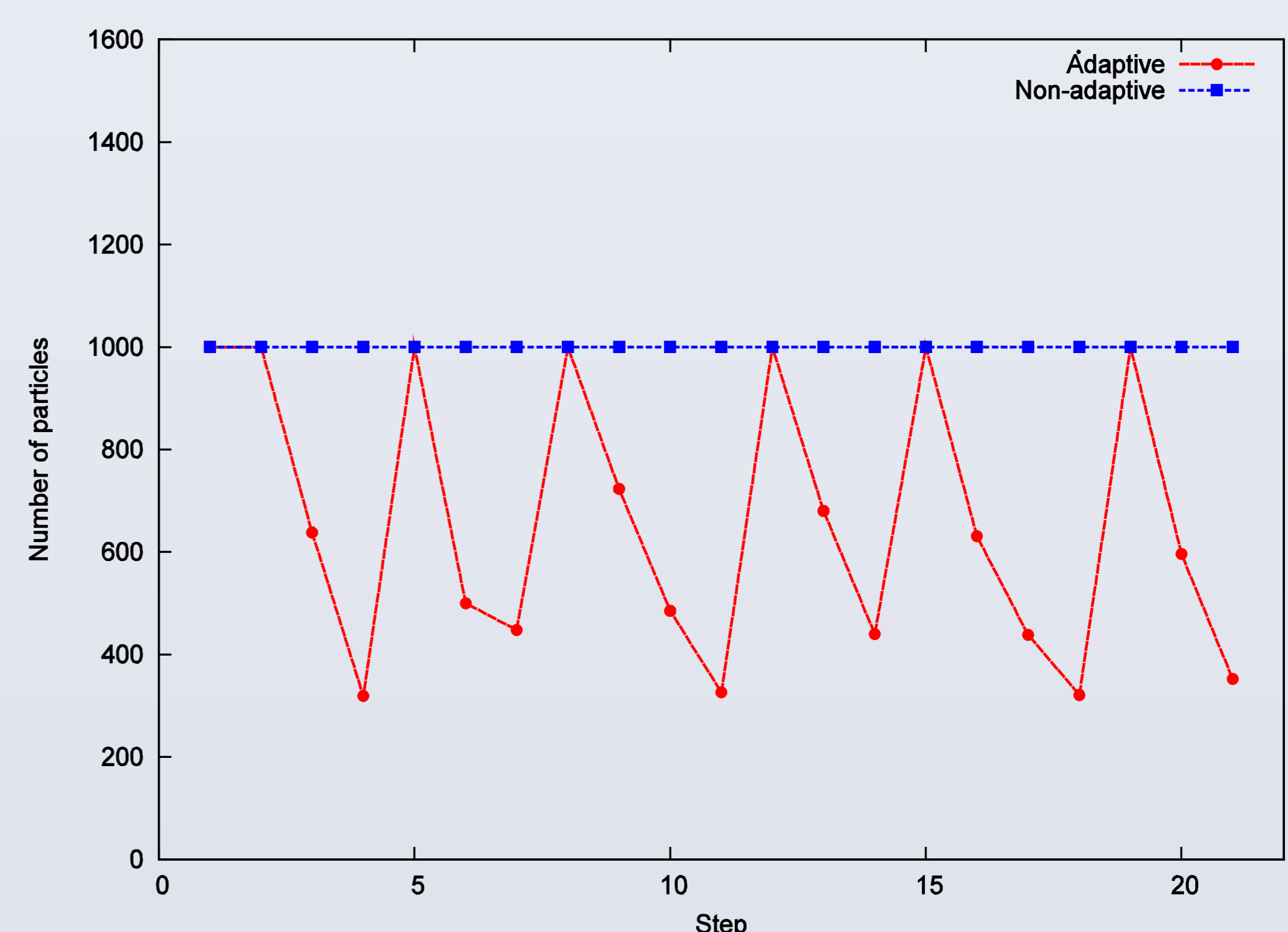
- PE^n - The n th processor.
- S^n - Speed of PE^n .
- PW^n - Power of PE^n .
- ρ^n - Number of particles distributed to PE^n .
- P - Total number of particles.
- T_{RT} - Real-time constraint.

Results

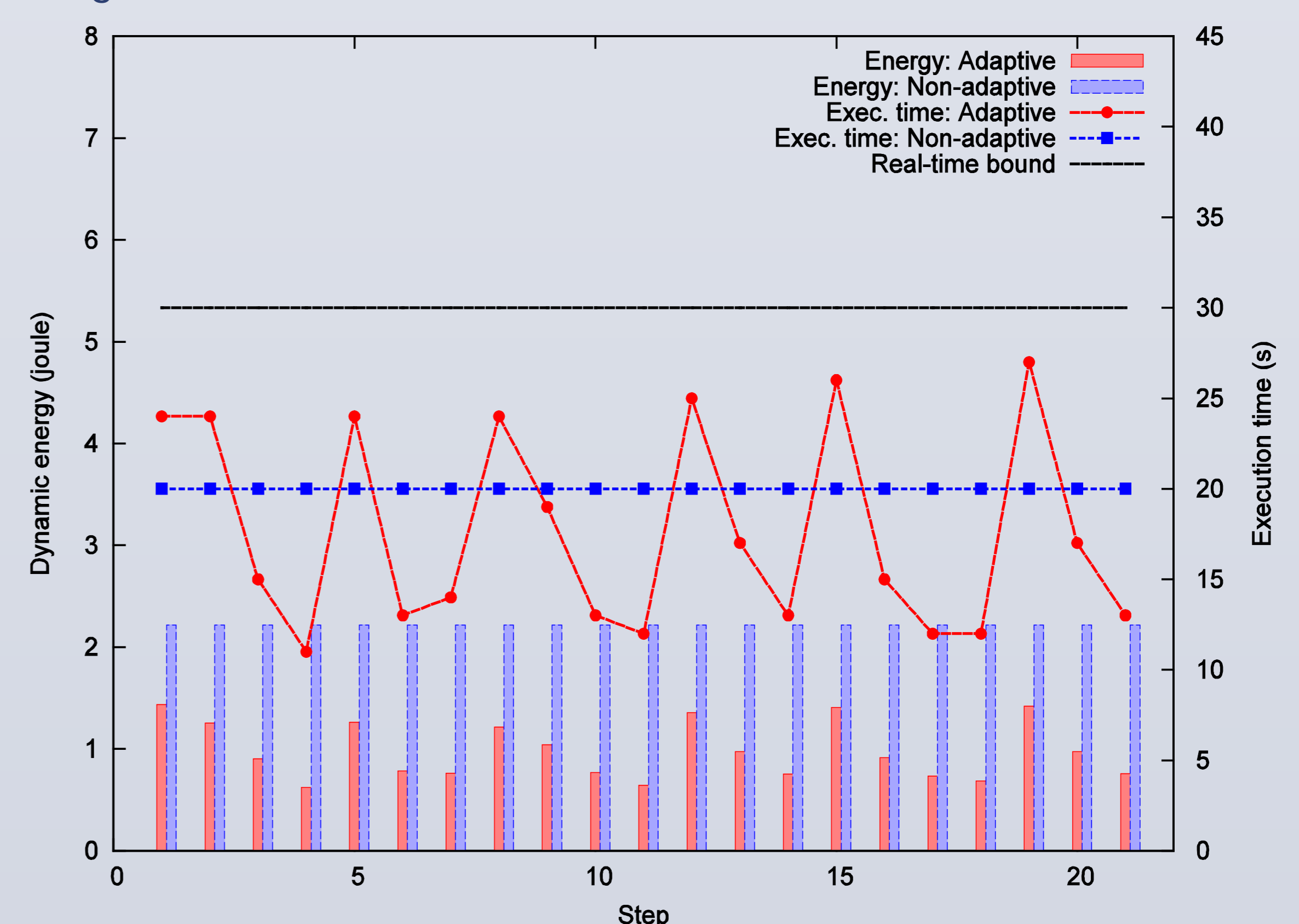
- Platform: Altera DE4 development board with a Stratix IV EP4SGX530 FPGA running at 100MHz.
- Example application: localisation of mobile robots.
- More particles are need for global positioning than local tracking.



- Computational complexity: reduced as the size of particle set changes dynamically.



- Dynamic energy consumption: reduced by 35-70%.
- Timing constraint: satisfied.



Summary

- Estimate states of dynamic systems: weighted particles.
- Dynamic workload: run-time task allocation to processors.
- Reduced energy: timing and quality of results maintained.

[1] M. Happe, E. Lubbers, and M. Platzner, "A Multithreaded Framework for Sequential Monte Carlo Methods on CPU/FPGA Platforms," International Workshop on Applied Reconfigurable Computing, 2009.

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